

## Colloquium

# Global Secure Sets of Graphs and its Applications

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摘要：

If  $G$  is a graph and  $v$  is a vertex of  $G$ , then  $N(v)$  denotes the neighborhood of  $v$  in  $G$  and  $N[v]$  denotes the closed neighborhood of  $v$  in  $G$ . Given a nonempty subset  $S$  of  $V(G)$ , a function  $A$  defined on  $S$  is called an *attack* on  $S$  in  $G$  if  $A(u) \subseteq N(u) - S$  for any  $u \in S$  and  $A(u) \cap A(v) = \emptyset$  for any distinct  $u, v$ . And a function  $D$  defined on  $S$  is called a *defense* of  $S$  if  $D(u) \subseteq N[u] \cap S$  for any  $u \in S$  and  $D(u) \cap D(v) = \emptyset$  for any distinct  $u, v$ . The set  $S$  is called a *secure set* of  $G$  if for each attack  $A$  on  $S$ , there exists a defense  $D$  of  $S$  such that  $|D(u)| \geq |A(u)|$  for any  $u \in S$ .

One can think the vertices of  $A(u)$  as attackers of  $u$  and those of  $D(u)$  as defenders of  $u$ . The attack is thwarted if  $|D(u)| \geq |A(u)|$ . For a secure set  $S$ , each attack on  $S$  can be thwarted.

A subset  $D$  of  $V(G)$  is called a *dominating set* of  $G$  if every vertex not in  $D$  is adjacent to at least one member of  $D$ . A subset  $S$  of  $V(G)$  is called a *global secure set* of  $G$  if it is a secure set of  $G$  and also a dominating set of  $G$ .

In this talk, I will introduce the ideas used in the study of global secure sets. And I will present some recent results and applications of global secure sets.